

# Efficient Cut-off Threshold Estimation for Word Spotting Applications

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**Abstract**— Word spotting is an alternative methodology for document indexing based on spotting words directly on document images with the help of efficient word matching while avoiding conventional OCR procedure. The result of the word spotting procedure is a list of word images ranked according to a certain similarity criterion. In this paper, we propose an efficient method to cut-off the ranked list in order to provide the best tradeoff between recall and precision rates. Our aim is to filter the most relevant results based on a threshold which corresponds to an approximate maximization of the expected  $F$ -Measure. This is achieved by introducing an estimator that combines the distance of each ranked word with its cumulative moving average. Experimental results on a database with representative historical printed documents prove the efficiency of the proposed approach.

**Keywords** word spotting; cut-off threshold; document indexing

## I. INTRODUCTION

Quick and efficient content exploitation is an important feature for any information system that provides access to historical document collections. Such collections usually contain a large number of documents and a robust indexing methodology is an essential performance and efficiency indicator. Due to document degradations, OCR systems often fail to support a correct segmentation of the printed historical documents into individual characters. Word spotting is a content-based retrieval procedure that spots words directly on document images with the help of efficient word matching while avoiding conventional OCR procedures [1], [2]. In the case of historical documents, Rath and Manmatha [3] presented a word matching scheme where noisy handwritten document images are preprocessed into one-dimensional feature sets and compared using the DTW algorithm. Rath et al. [4] present a method for retrieving large collections of handwritten historical documents using statistical models. Lavrenko et al. [5] present a holistic word recognition approach for handwritten historical documents. The query comprises either an actual example from the collection of interest or it is artificially generated from an ASCII keyword. A crucial aspect in the retrieval procedure is the word image representation which relies upon robust features. The retrieval procedure is based on a similarity criterion to be maximized or a distance measure to be minimized [6]. A common approach is to reduce the word representation into a fixed-length vector of features and use

geometric distance measures like euclidean, cosine, etc [2][7].

Word spotting produces a list of word images that are ranked according to their distance when compared to the query keyword. An important issue that arises is the proper separation of the ranked results into relevant and irrelevant word instances. This will help to provide the user with only the relevant results in a way that is convenient for searching purposes (e.g. extracting a list of document pages that include one or more instances of the query keyword). Clearly, a fixed similarity threshold cannot be applied since the distribution of distance values obtained may vary when applied to different datasets. In this paper, we propose a method for the determination of a cut-off threshold which is based on an estimator that combines the distance of each ranked word with its cumulative moving average. The efficiency of the proposed method is demonstrated showing that the local maximum of the estimator is highly correlated to the overall maximum of the expected  $F$ -Measure.

The remainder of this paper is organized as follows: Section II describes the word spotting system. In Section III the proposed methodology is detailed. Section IV presents evaluation results on representative historical documents while in Section V the conclusions are drawn.

## II. WORD SPOTTING SYSTEM

The main stages of a word spotting system are (a) word segmentation (b) feature extraction and (c) matching and ranking. In this section we describe how we implemented the main word spotting stages.

### A. Word segmentation

The word segmentation of the document pages is performed using the Run Length Smoothing Algorithm (RLSA) [9] which uses dynamic parameters that depend on the average character height as described in [10]. RLSA examines the white runs existing in the horizontal and vertical directions. For each direction, white runs with length less than a threshold are eliminated. The horizontal length threshold is experimentally defined as 50% of the average character height while the vertical length threshold is defined as 10% of the average character height.

### B. Feature extraction

The segmented words of the historical document as well as the query keyword are described by feature vectors which

are used during the matching phase in order to measure similarity between word images. Several features and methods have been proposed in the literature for word image matching based on strokes, contour analysis, etc. [11], [2].

In the proposed approach, two different types of features are combined providing a hybrid features vector for each dataset word as well as for the query keyword [12]. The first one divides the word image into a set of zones and calculates the density of the character pixels in each zone. The second type of features is based on word (upper/lower) profile projections. The word image is divided into two sections with respect to the horizontal line that passes through the center of mass of the word image. Upper/lower word profiles are computed by recording, for each image column, the distance from the upper/lower boundary of the word image to the closest character pixel.

### C. Word matching and ranking

The process of word matching involves the comparison/matching between the query keyword image and all the segmented words. Each word image  $w_i$  in the document corpus is represented by a feature vector  $\mathbf{p}_i$ ,  $1 \leq i \leq N$  in the  $k$ -dimensional feature space, where  $N$  equals the overall number of words in the dataset. All the words are ranked according to their distance to the  $k$ -dimensional feature vector  $\mathbf{q}$  that represents the input query. The top entries of the ranked list have the smallest distance values and correspond to words that are more similar to the query. As distance metric the cosine similarity is used:

$$d_i = 1 - \frac{\sum_{j=1}^k p_{ij} q_j}{\sqrt{\sum_{j=1}^k p_{ij}^2 \sum_{j=1}^k q_j^2}} \quad (1)$$

where  $p_{ij}$  and  $q_j$  are the  $j$ -th features of  $\mathbf{p}_i$  and  $\mathbf{q}$ , respectively.

## III. CUT-OFF THRESHOLD DETERMINATION

### A. The $F$ -Measure metric

Several methods have been proposed for evaluating the performance of the retrieval system [13], [14]. A well known performance measure is the  $F$ -Measure  $FM$  which provides a certain tradeoff between specificity and sensitivity. Taking into consideration the top  $i$  word instances,  $FM_i$  is expressed as the harmonic mean of precision  $P_i$  and recall  $R_i$  metrics as follows

$$FM(i) = \frac{2P_i R_i}{P_i + R_i} \quad (2)$$

Precision  $P_i$  is defined as the number of retrieved relevant word instances divided by index  $i$ , while recall  $R_i$  is defined as the number of relevant word instances divided by the total number of existing relevant words in the dataset. In a typical

retrieval scenario, precision is high in the top ranked positions and diminishes gradually while recall follows the reverse direction.  $F$ -Measure provides a certain tradeoff between recall and precision with its maximum value indicating the index for which the highest accuracy is achieved.

Fig. 1 demonstrates an example regarding query keyword "famille". The words in the dataset are ranked according to their distance  $d_i$  from the query. A subset of the top 50 results is shown in Table I. It can be seen that the top ranking positions are occupied by relevant word instances while irrelevant results start to emerge gradually as the ranking index increases. The maximum value of  $F$ -Measure  $FM_{opt}=0.695$  appears for index  $i_{opt}=48$ . It is the ranking position that provides the best tradeoff between recall and precision.



Figure 1. Query keyword "famille"

TABLE I. PRECISION, RECALL AND  $F$ -MEASURE VALUES FOR SOME OF THE TOP 50 RESULTS OF QUERY KEYWORD "FAMILLE"

| Rank $i$ | Word Instance   | Distance $d_i$ | Precision $P_i$ | Recall $R_i$ | $F$ -Measure $FM(i)$ |
|----------|-----------------|----------------|-----------------|--------------|----------------------|
| 1        | <b>famille</b>  | 0.088          | 1.000           | 0.021        | 0.042                |
| 2        | <b>famille</b>  | 0.090          | 1.000           | 0.043        | 0.082                |
| 3        | <b>famille</b>  | 0.096          | 1.000           | 0.064        | 0.120                |
| ...      | ...             | ...            | ...             | ...          | ...                  |
| 21       | <b>famille</b>  | 0.115          | 0.857           | 0.383        | 0.529                |
| 22       | <b>hostile</b>  | 0.116          | 0.818           | 0.383        | 0.522                |
| 23       | <b>famille</b>  | 0.118          | 0.826           | 0.404        | 0.543                |
| ...      | ...             | ...            | ...             | ...          | ...                  |
| 45       | <b>tandis</b>   | 0.157          | 0.689           | 0.660        | 0.674                |
| 46       | <b>famille</b>  | 0.159          | 0.696           | 0.681        | 0.688                |
| 47       | <b>honnête</b>  | 0.160          | 0.681           | 0.681        | 0.681                |
| 48       | <b>famille</b>  | <b>0.160</b>   | <b>0.688</b>    | <b>0.702</b> | <b>0.695</b>         |
| 49       | <b>laquelle</b> | 0.161          | 0.673           | 0.702        | 0.688                |
| 50       | <b>laquelle</b> | 0.162          | 0.660           | 0.702        | 0.680                |
| ...      | ...             | ...            | ...             | ...          | ...                  |

It should be noticed that the actual relevant words are given by the ground truth during the evaluation process and are not known before hand. Our intention is to determine a cut-off threshold index  $i_{cut}$  for which  $FM(i_{cut})$  is as close as possible to the expected maximum  $F$ -Measure score  $FM_{opt}$ .

### B. The cut-off threshold

In order to determine the cut-off threshold which approximately maximizes the expected  $F$ -Measure we introduce an estimator  $f_i$  that combines the distance  $d_i$  of the  $i$ -th ranked word with its cumulative moving average. Let

$$f_i = \frac{d_i}{c_i} \quad (3)$$

where

$$c_i = \frac{1}{i} \sum_{j=1}^i d_j \quad (4)$$

is the cumulative moving average. For  $i > 1$  the  $i$ -th value of  $c_i$  can be calculated recursively by the current  $d_i$  value and the previous  $c_{i-1}$  as follows

$$c_i = \frac{d_i + (i-1)c_{i-1}}{i} \quad (5)$$

Fig. 2 depicts  $d_i$ ,  $c_i$  and  $f_i$  for all the  $N$  ranked words in the dataset. It can be seen that the distance values  $d_i$  grow rapidly up to a value ( $\sim 0.2$ ) and then there is a large amount of words whose distance from the query is between 0.2 and 0.4. For the last ranked words the distance is exponentially increasing again. The values of  $f_i$  reach an overall maximum for  $i=N$  that equals

$$\|f\|_{\infty} = f_N = \frac{Nd_N}{c_N} \quad (6)$$

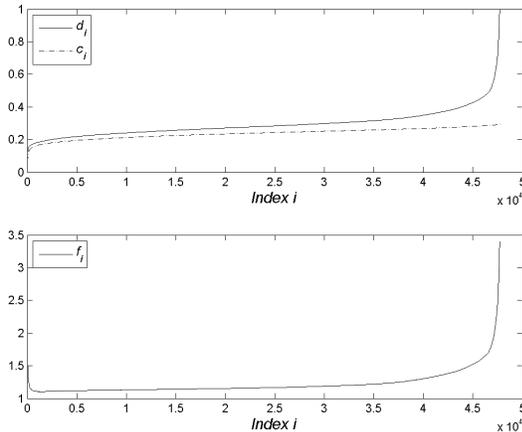


Figure 2. Values of  $d_i$ ,  $c_i$  and  $f_i$  for all the words in the dataset.

Besides its overall maximum,  $f_i$  reaches a local maximum for relatively small values of index  $i$ . This can be seen more clearly in the example of Fig. 3 which focuses on the vicinity

of the top ranked words. Both  $d_i$  and  $c_i$  are monotonically non-decreasing curves and the local maximum of  $f_i$  appears when their ratio is maximized, as shown in the bottom subplot of Fig. 3.

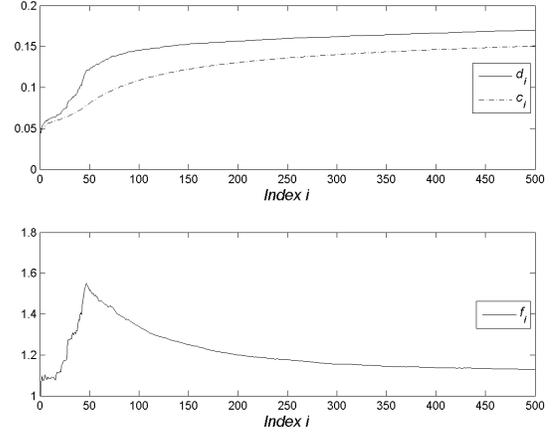


Figure 3. Values of  $d_i$ ,  $c_i$  and  $f_i$  for the top  $r=500$  ranked words.

We have noticed that setting the cut-off threshold  $i_{cut}$  equal to the index that locally maximizes  $f_i$  provides a good estimation of the expected maximum  $F$ -Measure, that is

$$i_{cut} = \arg \max_{i \in [1..r]} (f_i) \quad (7)$$

where  $f_i$  is considered in the vicinity of the top  $r$  words. Index  $r$  is determined by the ranking position that corresponds to the word whose distance is closest to the mean word distance. As mean word distance  $d_m$  we denote the cosine distance of the query vector  $q$  from a vector  $m$  whose  $j$ -th element equals the mean  $j$ -th feature of all the word feature vectors. That is,

$$r = \arg \min_i (|d_i - d_m|) \quad (8)$$

where

$$d_m = 1 - \frac{\sum_{j=1}^k m_j q_j}{\sqrt{\sum_{j=1}^k m_j^2 \sum_{j=1}^k q_j^2}} \quad (9)$$

and

$$m = (\bar{p}_1, \bar{p}_2, \dots, \bar{p}_k) \quad (10)$$

Fig. 4 depicts an example where the maximum of  $F$ -Measure appears at index  $i_{opt} = \arg \max (FM_{opt}) = 43$  and equals  $FM_{opt} = 0.805$  while  $i_{cut} = 47$  and  $FM(i_{cut}) = 0.79$ . Even when

indexes  $i_{cut}$  and  $i_{opt}$  differ significantly, as shown in the example of Fig. 5 the corresponding  $F$ -Measure values are highly correlated.

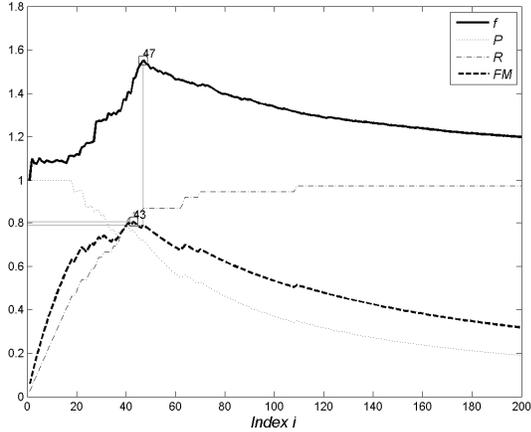


Figure 4. The maximum of  $F$ -Measure is at index  $i_{opt}=43$  and equals  $FM_{opt}=0.805$ . The cut-off threshold is  $i_{cut}=47$  and corresponds to  $F$ -Measure  $FM(i_{cut})=0.79$ .

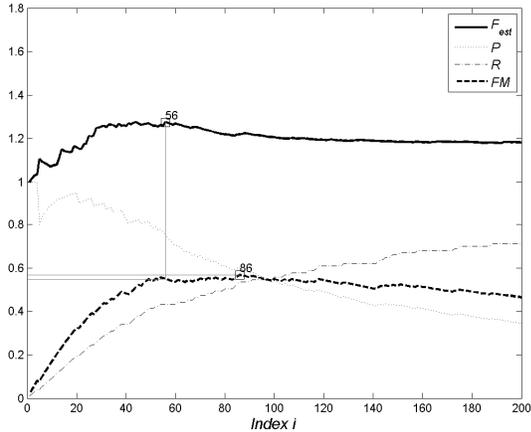


Figure 5. The maximum of  $F$ -Measure is at index  $i_{opt}=86$  and equals  $FM_{opt}=0.568$ . The cut-off threshold is  $i_{cut}=56$  and corresponds to  $F$ -Measure  $FM(i_{cut})=0.549$ , very close to  $FM_{opt}$ .

#### IV. EXPERIMENTAL RESULTS

We tested our methodology on a French historical book which was published in 1838 and is owned by Bibliothèque Nationale de France. In Fig. 6 a sample image is shown. We selected 153 pages from this book that contain an overall of 47715 words. We manually marked the ground truth for 20 keywords that have a variety of instances ranging from 33 up to 362, as shown in Table II.

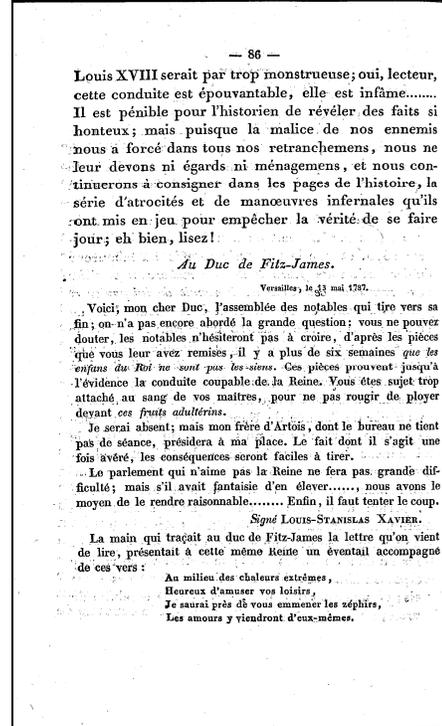


Figure 6. A document image sample

TABLE II. QUERY KEYWORDS AND THEIR INSTANCES

| Keyword        | Instances | Keyword        | Instances |
|----------------|-----------|----------------|-----------|
| <b>avait</b>   | 121       | <b>jamais</b>  | 55        |
| <b>bien</b>    | 97        | <b>justice</b> | 44        |
| <b>comme</b>   | 102       | <b>Louis</b>   | 156       |
| <b>contre</b>  | 52        | <b>Madame</b>  | 39        |
| <b>dans</b>    | 325       | <b>mort</b>    | 51        |
| <b>fait</b>    | 104       | <b>plus</b>    | 196       |
| <b>famille</b> | 47        | <b>pour</b>    | 362       |
| <b>France</b>  | 44        | <b>Roi</b>     | 56        |
| <b>homme</b>   | 39        | <b>sans</b>    | 97        |
| <b>hommes</b>  | 33        | <b>tous</b>    | 102       |

For each query keywords the precision  $P$ , recall  $R$ , and  $F$ -Measure curves are calculated according to the ground truth. Based on these measures, the maximum value  $FM_{opt}$  of  $F$ -Measure and its index  $i_{opt}$  are determined. The index  $i_{cut}$  of  $f_i$  is given by (7) and the corresponding  $F$ -Measure value  $FM(i_{cut})$  is also calculated. The results for all the query keywords are shown in Table III. The last column presents the efficiency of  $FM_{opt}$  approximation. The experimental results show that the proposed estimator  $f$  shows a consistency in approximating the  $FM_{opt}$  value. Moreover,  $f$  does not depend on the ranking position of index  $i_{cut}$ . Indeed,

there are cases where  $i_{cut}$  and  $i_{opt}$  are nearby indexes and  $FM(i_{cut})$  provides an almost perfect approximation of  $FM_{opt}$  regardless if  $i_{cut}$  points to a small cut-off threshold (e.g.  $i_{cut}=44$  for “contre”) or it indicates a much higher threshold (e.g.  $i_{cut}=140$  for “Louis”). Even more interesting are cases where despite that indexes  $i_{cut}$  and  $i_{opt}$  differ significantly (e.g. “bien” and “tous”),  $FM(i_{cut})$  still provides a good approximation to the maximum  $F$ -Measure value. Even in case of keyword “avait”, where index  $i_{cut}$  is almost two times larger than  $i_{opt}$ , the estimation error remains low, i.e. about 11% of  $FM_{opt}$ . The overall experimental results show that the average estimation error is below 8% in terms of  $F$ -Measure.

TABLE III. APPROXIMATION EFFICIENCY FOR SEVERAL CUT OFF THRESHOLDS

| Query                | $i_{opt}$ | $FM_{opt}$ | $i_{cut}$ | $FM(i_{cut})$ | $FM(i_{cut})/FM_{opt} * 100$ |
|----------------------|-----------|------------|-----------|---------------|------------------------------|
| <b>avait</b>         | 85        | 0.495      | 160       | 0.441         | 89.12%                       |
| <b>bien</b>          | 86        | 0.568      | 56        | 0.549         | 96.61%                       |
| <b>comme</b>         | 98        | 0.770      | 100       | 0.762         | 99.01%                       |
| <b>contre</b>        | 43        | 0.863      | 44        | 0.854         | 98.96%                       |
| <b>dans</b>          | 272       | 0.807      | 403       | 0.709         | 87.79%                       |
| <b>fait</b>          | 69        | 0.358      | 240       | 0.291         | 81.11%                       |
| <b>famille</b>       | 48        | 0.695      | 46        | 0.688         | 99.06%                       |
| <b>France</b>        | 19        | 0.413      | 25        | 0.377         | 91.30%                       |
| <b>homme</b>         | 17        | 0.500      | 12        | 0.431         | 86.27%                       |
| <b>hommes</b>        | 27        | 0.700      | 16        | 0.612         | 87.46%                       |
| <b>jamais</b>        | 53        | 0.519      | 43        | 0.469         | 90.52%                       |
| <b>justice</b>       | 31        | 0.480      | 45        | 0.449         | 93.63%                       |
| <b>Louis</b>         | 136       | 0.897      | 140       | 0.892         | 99.40%                       |
| <b>Madame</b>        | 43        | 0.805      | 47        | 0.791         | 98.24%                       |
| <b>mort</b>          | 34        | 0.706      | 38        | 0.697         | 98.69%                       |
| <b>plus</b>          | 140       | 0.821      | 157       | 0.805         | 97.94%                       |
| <b>pour</b>          | 381       | 0.770      | 515       | 0.673         | 87.39%                       |
| <b>Roi</b>           | 51        | 0.748      | 53        | 0.734         | 98.17%                       |
| <b>sans</b>          | 68        | 0.727      | 187       | 0.570         | 78.43%                       |
| <b>tous</b>          | 144       | 0.528      | 115       | 0.525         | 99.41%                       |
| <b>Total average</b> |           |            |           |               | <b>92.93%</b>                |

## V. CONCLUSIONS

This paper proposes an efficient method for the estimation of a cut-off threshold that can be applied to the ranked results list of a word spotting system in order to filter the most relevant words. As a performance measure, the  $F$ -Measure is used which provides a certain tradeoff between specificity and sensitivity. The method is based on an estimator that for each ranked word combines its distance with its cumulative moving average. The estimator has a

local maximum which is highly correlated to the overall maximum of the expected  $F$ -Measure. Experiments on a database with representative historical printed documents evidenced promising results that demonstrate the feasibility of the proposed method.

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